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Documentos de Trabajo del Banco Central de Chile Working Papers of the Central Bank of Chile Agustinas 1180, Santiago, Chile Teléfono: (56-2) 3882475; Fax: (56-2) 38822311 Documento de Trabajo Nº 984 Working Paper N° 984

# Heterogeneous Impacts of Commodity Price Shocks on Labour Market Outcomes: Evidence and Theory for the Chilean Mining Sector\*

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#### Abstract

Using data for the Chilean mining sector, we provide SVAR evidence accounting that commodity price shocks have distributional consequences at business cycles frequencies in a small open economy. We show that an unexpected impulse in commodity prices increases the wage premium between high and low-skilled workers and, at the same time, it decreases the employment level ratio between high skilled and low skilled workers. In order to rationalize this findings, we build a DSGE-SOE model with asymmetric search and matching (SAM) frictions. The theoretical model, calibrated and estimated with Chilean data, achieves to replicate the empirical labour market dynamics that come from an unexpected increase in the commodity price for the small open economy. Besides, we find that the principal parameters that determine how the commodity shock is going to affect labour market outcomes between high and low-skilled workers are the Nash bargaining power of workers, and the skill intensity in commodity production. The former affects the distribution of wages, and the latter affects the employment level distribution among high and low-skilled workers.

#### Resumen

Usando datos para el sector minero chileno, proporcionamos evidencia SVAR que explica que los *shocks* de precios de las materias primas tienen consecuencias distributivas a nivel de ciclo económico en una economía pequeña y abierta. Mostramos que un impulso inesperado en los precios de las materias primas aumenta la prima salarial entre los trabajadores de alta y baja calificación y, al mismo tiempo, disminuye la razón de nivel de empleo entre los trabajadores de alta y baja calificación. Para racionalizar estos hallazgos, construimos un modelo DSGE-SOE con fricciones asimétricas de búsqueda y emparejamiento. El modelo teórico, calibrado y estimado con datos chilenos, logra replicar la dinámica empírica del mercado laboral que proviene de una aumento inesperado en el precio de las materias primas para la pequeña economía abierta. Además, encontramos que los principales parámetros que determinan cómo afectaría el *shock* de las materias primas los resultados del mercado laboral entre trabajadores y la intensidad de la calificación en la producción de materias primas. El primero afecta la distribución de salarios, y el segundo afecta la distribución del nivel de empleo entre trabajadores de alta y baja calificación.

<sup>\*</sup>This paper was partially funded by Beca de Doctorado CONICYT. Folio: 21191751. Valenzuela gratefully aknowledges the financial support from FONDECYT grant project 1191888. We also want to thank the Economics Department seminar at FEN, Universidad de Chile. The views expressed are those of the authors and do not necessarily represent the views of the Central Bank of Chile or its board members. †josvalenzu@fen.uchile.cl; ‡dcoble@bcentral.cl.

# 1 Introduction

The ups and downs of commodity prices have caught wide attention on macroeconomists in the last two decades. Fernández, González and Rodríguez (2015)[10] have described this phenomenon as a commodity price *roller coaster*. The latter has awaken interest on the effects that commodity price shocks have on domestic economic outcomes. In this regard, there is some consensus that commodity price shocks have positive effects in the domestic economic environment for the exporting countries, as they yield aggregate demand expansions, increasing wages and employment, and real exchange rate appreciations (see Fornero, Kirchner and Yani (2015)[11], Medina and Soto (2016)[19], Bodenstein et.al (2017)[4]). While this view of the effects of commodity price shocks seem, somehow, uncontested, there is still no a clear answer to the question regarding how do these kind of shocks affect the different types of agents in the economy, specifically, on different types of workers, considering their wealth or skill (education) level.

To think about the latter, we must understand which mechanisms drive the propagation of commodity price shocks into the economy. There are several ways in which this may happen. The first one is directly into the commodity sector. Better future expectations on commodity prices increase investment projects and the reactivation of current ones on hold which increases the demand for workers within the sector (demand channel), but also they encourage negotiations between the worker unions within the sector and the firms' owners regarding salaries and bonuses (institutional channel). In second place is the indirect effect that commodity price shocks generate outside the commodity sector. Specifically, when commodity prices are higher the sector increases its demand for different kinds of goods and services in sectors such as energy, transport, engineering and consultancy, construction, among others. Workers of those sectors experience higher demand and, thus, higher wages. Third, we have that some commodity sectors are very important for fiscal revenues, such as oil in some Arabic countries or metal mining in Australia or Chile, as they are highly taxed or their production depends directly on public firms. In this regard, fiscal revenues from commodity production can increase employment and wages through, e.g., new public investment projects. Finally, another propagation channel may be the one proposed by Bodenstein et.al., (2017)[4], which consists in that commodity price increases yield a real appreciation of the exchange rate which, at the same time, lowers the relative price of domestic goods which increases their demand and, therefore, the labor demand and wages for workers in that sector of the economy. Whichever be the case, it is not obvious how do commodity price shocks affect different workers in the economy, mainly because they are not equal regarding the intensity in the production (commodity or not-commodity), their complementarity with capital, and the frictions they face in the labor market.

In this paper we address the question of which are the distributional conse-

quences on labor market outcomes for heterogeneous workers (differing in their skill level) that arise from commodity price shocks, focusing in the institutional and demand channels of the shock propagation. We propose a structural model with heterogeneous workers and labor market frictions which allows us to explain a novel stylized fact regarding the effect of copper price shocks on the employment and wage gap between high and low-skilled workers for the Chilean mining sector.

In order to motivate the discussion, the data shows a pattern regarding the relation between commodity prices against the wage premium and the employment ratio<sup>1</sup>. For the case of Chile, Figure 1 displays the detrended mining sector workers' wage premium and the copper price from the 2005-2019 time span. In can be seen that, overall, the wage premium increases when the copper price has experienced booms in the business cycle. This is specially true for the commodity price boom period, which spanned from 2003 to 2011. This evidence suggests that, over the business cycle, the wage premium and the copper price are positively correlated. In fact, the correlation between copper price and wage premium for the time span in Figure 1 is 0.11.

Figure 1: Copper price index (left) and detrended wage premium (right).



Source: Chilean Unemployment Benefit database and Central Bank of Chile

Regarding the relation between the employment ratio and the copper price over the business cycle for Chile, Figure 2 shows the detrended mining sector workers' employment ratio and the copper price for the 2005-2019 time span. In

 $<sup>^{1}</sup>$ The wage premium is defined as the high-skilled and low-skilled real wage ratio, while the employment ratio is defined as the high-skilled and low-skilled employment level ratio. Definitions for high and low-skilled workers are presented in Section 3.

contrast with Figure 1, it seems that the relation between the employment ratio and the copper price is negative, where in periods when copper price soared, the employment ratio experienced systematic downfalls. Contrary to Figure 1, the correlation between copper price and the employment ratio es -0.44.

Figure 2: Copper price index (left) and detrended employment ratio (right).



Source: Chilean Unemployment Benefit database and Central Bank of Chile

The evidence presented in Figures 1 and 2 is, somewhat, puzzling, because it seems that copper price shocks have different impacts on the employment ratio and wage premium. While, on the one hand, copper price shocks seem to increase the wage premium, on the other happens that copper price shocks decrease the employment ratio. This facts are not consistent with a neoclassical frictionless labor market model, as in Guerra-Salas (2018)[14], Pellandra, (2015)[20] and Benguria, Saffie and Urzua, (2018)[3], in which commodity price shocks affect the wage premium and the employment ratio in the same way through a demand channel.

Our methodology to give an answer on the issue is, first, by using Chilean time series on the mining sector we provide an SVAR analysis that formalizes the evidence presented above and gives some insights on how do copper price shocks affect labor market outcome gaps between high and low-skilled workers, specifically in the Chilean mining sector. The SVAR analysis shows that, consistent with previous studies, a copper price shock yields positive effects on aggregate demand and job vacancy creation which, at the same time, lowers unemployment levels. Regarding labor market outcome gaps, we find that H-to-L employment level gap (measured by the employment ratio between high and lowskilled workers) decreases on impact and this effect is persistent, lasting more than 10 quarters and, for the wage gap, it increases on impact and afterwards it tends to decrease, but the positive effect is relatively persistent. With this analysis on hand, we propose a DSGE-SOE (Dynamic Stochastic General Equilibrium for a Small Open Economy) model in order to rationalize the findings of our SVAR exercise. Our model features two main transmission channels of the commodity price shock in the domestic economy: (i) heterogeneous Search and Matching (SAM) frictions and, (ii) skill intensity in commodity production. Heterogeneous SAM frictions allow us to model the labor market taking account on the fact that high and low skilled workers face different labor institutions when searching for a job, and this conditions determine their final outcomes in unemployment and wages (Dolado et.al., (2021)[7]). Skill intensity in commodity production allows us to account for the fact that commodity production is more intensive in low-skilled workers. We show that our simple model is capable to rationalize quite well the dynamics presented by the SVAR exercise. Finally, we explore how do SAM frictions and skill intensity in commodity production interact in our model, in order to provide a complete answer on how the commodity price shock is transmitted in our framework.

We think that Chile provides a good setup to study the heterogeneous effects that commodity (specifically, copper) price shocks may have. First, Chile is the leading copper producer in the world by far, producing an estimated 5.7 billion metric tons of copper in 2020, which represents almost 30% of the global annual copper output. Second, the mining sector's contribution to the Chilean GDP is approximately 10%, and the industry represents about 50% of the country's total exports. These first two points translate into that mining activity and, specially, copper activity has huge participation in the Chilean economic output. In this regard, an economy that is highly exposed to commodity price shocks is a correct place to analyze how do fluctuations in commodity prices affect the heterogeneity in the labor market outcomes of the sector. And third, the Chilean mining sector features three characteristics that may affect labor outcome gaps in non-trivial ways when the copper price fluctuates: (i) highly intensive in low-skilled labor, (ii) high degree of capital-skill complementarity and, (iii) strong labor unions with high levels of worker participation across skill types. These features allow us to set up a structural model with labor market frictions in order to understand how the demand and institutional channel interact.

The reminder of the paper is organized as follows. Section 2 reviews the relevant literature. Section 3 provides with an empirical motivation of our question of interest for the Chilean case with an SVAR exercise. Section 4 presents the DSGE-SOE model with heterogeneous SAM frictions which has the goal of rationalize the evidence provided in Section 3. Section 5 and 6 do the calibration strategy and the parameter estimation of the model, respectively. Section 7 does the analysis of the model economy, going deeper in the main transmission mechanisms that drive the results of our model. Section 8 concludes the results of this study and derives policy implications and avenues for further research.

# 2 Literature Review

Our study is related to two strands of the literature. The first one is that which studies the relation between commodity price shocks and labor market inequality focusing in Latin American countries. Benguria, Saffie and Urzua (2018)[3] use administrative data for Brazil from 1999 to 2013 and show that increases in regional commodity prices reduce the skill premium in that particular location. A paper that proposes a theoretical approach to give an answer on which is the mechanism that drives the declining skill premium in Latin America is Guerra-Salas (2017). He proposes a DSGE-SOE model with two productive sectors: tradables and non-tradables. Under the calibrated parameters, the model shows that a commodity price shock reallocates labor from the tradable to the non-tradable sector and, with the assumption that the non-tradable sector is more intensive in low-skilled labor, this reallocation of labor input yields a decline in the skill premium. Also, there are two papers that use data from Chile to explain how is labor market inequality affected by commodity price shocks, specifically, copper price shocks. The first one is Pellandra (2015)[20] which studies the effect of commodity boom on the wages and employment of skilled and unskilled workers in Chile between 2003 and 2011. He finds that a copper price shock in an industry that employs intensively employs unskilled labor (as the commodity sector does) reduces local wage premia proportionally more in regions where that industry represents a higher share of total employment compared to other regions. Specifically, empirical results show that a region exposed to a 10% increase in average commodity prices experienced a 2.4% increase in average unskilled workers' wages relatively to other regions, and that such gains contributed to a reduction in regional wage premia. Finally, Álvarez, García and Ilabaca (2017)<sup>[1]</sup> perform a natural experiment with Chilean microdata and show that copper price shocks contributed to decrease the poverty rate for the period 2003-2013, which represented the great commodity boom period. Besides, they explain that a channel for poverty reduction was that of improving unskilled workers labor market outcomes, where they show that commodity price shocks had a positive impact on employment and wages, but particularly for unskilled workers in mining industries. Our study adds to this literature using data from an administrative record for a time span that goes beyond the commodity price boom (which ended in 2011-2012) and focusing on the Chilean copper sector. Narrowing the analysis to only the commodity sector allows us to disentangle the effect of multiple channels that act at the same time when there is an unexpected commodity price shock. In particular, we can assess the dynamics of such a shock that are particular to the Chilean mining sector in order to compare the role of the demand and labor market institutional channel in the determination of employment and wage outcomes within the sector.

The second strand of the literature with which this paper relates is the one that embeds the standard Diamond, Mortensen, Pissarides (DMP) framework into a model of the business cycle. Early contributions of this are Andolfatto (1996) and Merz (1995). However, open economy models rarely feature search and matching frictions in the labour market. Hairault (2002) and Campolmi and Faia (2011) show how augmenting a standard open economy model by the DMP framework impacts the transmission of shocks across countries. Christiano et al. (2011) develop a detailed small open economy DSGE model with search and matching frictions that can be employed for policy analysis. Boz et al. (2009) study search and matching frictions in a small open economy model calibrated to Mexican data. Bodenstein et.al., (2017)[4] investigate empirically and theoretically the connection between commodity price shocks and unemployment in advanced resource-rich small open economies within a DMP framework. They find that shocks to commodity prices are shown to influence labour market conditions primarily through the real exchange rate, whereas a positive price shock is found to expand the components of GDP, to cause the real exchange rate to appreciate, and to improve labour market conditions. We contribute to this strand by adding heterogeneity in workers' skills in the spirit of e.g., Dolado et al. (2021); Wolcott (2020); Abbritti and Consolo (2022). Workers with different skills face different labor market frictions and, also, they are employed with different intensity in the commodity production<sup>2</sup>. This framework allows us to rationalize the empirical fact documented here which states that, for the Chilean mining sector, the employment ratio and the wage premium exhibit a negative correlation in response to a copper price shock.

# 3 Commodity Price Shocks and Labour Market Outcomes Gap: SVAR Evidence

In order to motivate out research question, we start by identifying the impact of a positive commodity shock on the skill premium and the relative employment rates of high and low skilled workers in a SVAR model. We construct time series of both gap using the data of the *Chilean Unemployment Insurance* (UI) which is an administrative database, which has open source material for the 3, 5 and 12% of the whole sample. In this regard, we used the 3% sample, which comprehends 319,425 workers from 2002 to 2020 at a monthly frequency. Labour market data is extracted from this dataset as follows: we calculate wages and employment levels by skill level by obtaining quarterly averages for these variables from 2005:M1-2019M10. We classify workers as high or low skilled according to whether they have some college education or not. Specifically, a worker is considered high skilled if he has finished his college education or further, and is considered low skilled if he has incomplete college education or below. On the other hand, employment level is defined as the number of salaried

 $<sup>^{2}</sup>$ To illustrate, low-skilled workers represent more than 60% of the total mining sector workforce in Chile but, on the other hand, the mining sector is highly intensive in capital, which shows higher degrees of complementarity with high-skilled workers rather than with low-skilled workers.

workers in each skill category<sup>3</sup>.

We examine quarterly data covering the sample period between January 2005 to October 2019. We exclude the year 2020 and forth from the sample to exclude the COVID-19 crisis of 2020 which clearly had an effect in several labour market outcomes in the world, not only in Chile. Besides, we exclude years 2002, 2003 and 2004 from the sample because, as Cruz and Rau (2021)[6] argue, the UI system started in October 2002 with new job contracts, so the UI data have become more representative over time. In this regard, Schnbruch and Carranza (2015)[21] argue that in 2005 the workers in the UI database represented approximately 50% of all wage earners, reaching 80% of Chilean formal wage earners in 2012. For these reasons, and because the data that we use is a quarterly time-aggregate of the wages of workers over a certain period, which means that dropping years from the sample will leave us with less observations to perform the analysis, is that we decided to follow Cruz and Rau (2021)[6] and use the data of the UI base from 2005:M1.

One caveat regarding the UI database is that the observed wages may be truncated by a maximum wage cap that is used as a base for calculation of the monthly amount of the wage proportion that goes to the unemployment insurance savings for every formal worker. Regarding the latter, for the mining sector the UI database records that, since 2005, 20% of the observations are truncated by the wage cap imposed by the administrative entity<sup>4</sup>. This implies that for 80% of mining workers we observe their complete wages, while for the rest we only observe that they earn a wage that is above the cap, but not the received monthly wage itself. Disaggregating by skill level, we have that 41% and 15% of high and low-skilled workers, respectively, have their wages capped.

Our SVAR consists of seven variables: real GDP, the vacancy creation index, high-skilled workers real wage rate, the skill premium, high-skilled workers employment rate, the relative employment rate, and real copper price. Following Fornero et.al (2015)[11], we arrange the SVAR into two blocks: (i) a foreign block, and (ii) a domestic block. The only variable in (i) is the real copper price, and the rest variables listed above belong to the domestic block. Here, we assume that foreign variable does not respond to changes in domestic variables. The reduced-form VAR can be written as follows:

$$\begin{bmatrix} y_{1,t} \\ y_{2,t} \end{bmatrix} = \begin{bmatrix} c_1 \\ c_2 \end{bmatrix} + \begin{bmatrix} \boldsymbol{A}_1 & \boldsymbol{A}_2 \\ \boldsymbol{B}_1 & \boldsymbol{B}_2 \end{bmatrix} \times \begin{bmatrix} x_{1,t} \\ x_{2,t} \end{bmatrix} + \boldsymbol{D} \begin{bmatrix} z_{1,t} \\ z_{2,t} \end{bmatrix} + \begin{bmatrix} \varepsilon_{1,t} \\ \varepsilon_{2,t} \end{bmatrix},$$

where  $y_{1,t}$  and  $y_{2,t}$  are vectors of foreign variables and domestic variables,

<sup>&</sup>lt;sup>3</sup>In the literature, the employment level is obtained -in most cases- using the number of salaried workers times the average hours worked in some time span, e.g., a week or a month. We could not use use information for hours worked because the UI database does not contain that variable.

 $<sup>^{4}</sup>$ The wage cap has increased since 2005. In the early years of the implementation of the UI system the cap was of 90 U.F (Unidades de Fomento), and it has increased systematically to 118.9 U.F in 2019. The U.F is an inflation indexed monetary unit which is used in Chile to set a number of contracts such as e.g., labor, housing, or savings contracts.

respectively. Outcomes are explained by previous developments measured by p lags in the variables  $y_{1,t-1}, ..., y_{1,t-p}$  and similarly for  $y_2$ . Lagged information is gathered in  $x_{1,t}$  and  $x_{2,t}$ . In addition, vector  $z_t$  includes deterministic terms such as time trends and constants. The unknown coefficients to be estimated are the elements of the vectors  $c_1$  and  $c_2$  and the matrices  $A_1, A_2, B_1, B_2$  and D. The error vector is defined by  $\varepsilon_t$ , where they are expected to by zero on average and their variance-covariance matrix is positive definite.

The VAR is restricted to reflect the small open economy assumption, that is, we impose that  $A_2 = 0$  such that  $y_1$  forms an exogenous block of variables (which will be subject to the identification scheme that we describe below). Data for real GDP, the vacancy creation index and real copper price were drawn from the Central Bank of Chile's statistics center. Using different information criteria (AIC, HQIC, and BIC) we include one lag of each variable in the VAR.

The strategy that we use here in order to identify real copper price shocks is through a lower triangular Cholesky decomposition. The identifying assumptions are that the copper price affects contemporaneously every variable in the system, while copper price do not react to any impulse in the other variables within a quarter. The ordering of the endogenous variables in the SVAR is as follows: the copper price shock affects GDP, then GDP affects vacancy creation, vacancy creation affects the high-skilled employment rate whereas this variable affects the high-skilled real wage rate, and finally this las variable affects the wage premium. In more detail, the vector of orthogonalized shocks,  $\boldsymbol{\nu}_t$ , is defined by

$$\boldsymbol{\nu}_{t} = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ a_{21} & 1 & 0 & 0 & 0 \\ a_{31} & a_{32} & 1 & 0 & 0 \\ a_{41} & a_{42} & a_{43} & 1 & 0 \\ a_{51} & a_{52} & a_{53} & a_{54} & 1 \end{pmatrix} \begin{pmatrix} \varepsilon_{pCO} \\ \varepsilon_{GDP} \\ \varepsilon_{vac} \\ \varepsilon_{emp} \\ \varepsilon_{wage} \end{pmatrix}$$

In what follows, we present two different SVAR exercises. First, we only consider labor outcomes for the mining sector. That is, the employment ratio and the skill premium are exclusively considering workers from the mining sector. This will give us a notion regarding the impact of a positive real copper price shock on workers from a sector that is highly exposed to commodity price fluctuations. The second exercise is leaving aside mining sector workers and, thus, only considering workers from the non-mining sector. Jointly, these exercises will provide us with the different impacts that the commodity and non-commodity sectors experience after a commodity (copper, specifically) price shock. That is, we will be able to explore if there is any difference in how the employment ratio and the wage premium react in both sectors.

#### 3.1 SVAR for the mining sector



Figure 3: IRFs to an unexpected increase in the international copper price.

Figure 3 displays point estimates and 68 percent confidence intervals for the impulse response functions (IRFs) of the baseline SVAR model to the identified real copper price shock. The shock has expansionary effects. After the unexpected copper price increase, total GDP increases persistently. Regarding the labour market variables, the vacancy creation index presents an important increase on impact, returning to its steady state level after, approximately, 10 quarters. On the other hand, the employment ratio decrease significantly on impact and it returns to its steady state level after, approximately, 13 quarters. Finally, the wage premium, despite of its decrease on impact, it increases after the first quarter until the 10th quarter, where it returns to its steady state value. Overall, the reported IRFs suggest that the gap between high-skilled and lowskilled workers in terms of employment rates is negatively related to an unexpected increase in the copper price, whereas regarding wages the opposite happens. In other words, low-skilled workers are more benefited by an unexpected copper price shock than high-skilled workers regarding their employment level, but high-skilled workers are more benefited by the shock regarding wages. At the peaks of the IRFs, the employment rate decreases by about 3 percentage points, while the wage premium increases by around 5 percentage points. Figure 24 in the appendix displays the result for this same exercise but using the UI database for the 20% of the whole pool of Chilean mining sector formal workers. The results are qualitatively the same.

#### 3.2 SVAR for the non-mining sector

Figure 4: IRFs to an unexpected increase in the international copper price.



Figure 4 displays point estimates and 68 percent confidence intervals for the impulse response functions (IRFs) of the counterfactual SVAR model to the identified real copper price shock considering labor market variables for workers outside the mining sector. The results are similar with the ones presented in Figure 3; real GDP and vacancies increase as well, but the shock is less persistent, that is, these variables return to their steady-state values faster than for the mining sector, and the effect is only significant during the first 2 or 3 quarters after the impact. Regarding the employment ratio, it decreases as well, getting to a lower bound near of the third quarter after the impact, and returning to its steady-state level approximately after eight quarters. The most remarkable difference between Figures 3 and 4 lies in the wage premium. In the latter, the copper price shock is only statistically significant on-impact and from the first quarter after the shock onwards the wage premium response is not statistically different than 0.

The results in Figure 4 suggest that the effects of a copper price shock outside the mining sector are -qualitatively- similar regarding the employment ratio, but different regarding the wage premium. Here, we can go back to Alvarez et. al (2017)[1] and add that they do not make the difference we make here regarding which subset of workers are included in the analysis. Specifically, they do not condition their analysis on workers that belong -or not- to the commodity (mining) sector. Considering the latter, it is reasonable that the results presented in Figure 4 are similar to those presented in Alvarez et.al (2017)[1], since workers in the mining sector represent about 3% of the total employed workers according to the CASEN survey conducted in 2017.

Summarizing, it seems that a copper price shock decreases the employment ratio inside and outside the mining sector, but it increases the wage premium inside the mining sector and shows mild effects outside it.

With these results in hand, in the next section we present a DSGE-SOE model with SAM frictions in order to rationalize the findings of the SVAR evidence presented above. The novel evidence presented here for the mining sector regarding the negative correlation between the response of the wage premium and the employment ratio to a copper price shock motivates the use of labor market frictions in the structural model, whereas a model without frictions or wage rigidities is only capable to capture the demand effect of a productivity shock.

# 4 The Model

Our model belongs to the family of DSGE models with SAM frictions for an small open economy (SOE), which we will refer to as DSGE-SOE. We omitted the New Keynesian feature from the model because our interest is to analyze the impact of commodity price shocks in real variables, and not in nominal variables, therefore nominal rigidities become less relevant in an environment like this. On the other hand, SAM frictions allow us to model unemployment. Workers in the household may work in the commodity sector or in the consumption goods sector. The fraction of commodity sector workers within the representative household is denoted by  $x \in (0, 1)$ . There is heterogeneity in skills in workers that belong to the commodity sector. We model this heterogeneity as follows: each household has a fixed proportion of low skilled labor market participants, which may be employed or unemployed. This proportion  $(1 - \pi)$  of high-skilled labor market participants. The latter is depicted in Figure 25 in the appendix.

Heterogeneity in skills also imply that workers of different type will face different labor market frictions (*asymmetric* SAM) and in their role in production as well. The latter means that only workers which belong to the commodity sector will face SAM frictions. Also, the representative household has access to the international financial market, where it can buy and sell one-period risk-free foreign bonds.

There is a perfectly competitive firm that produces a homogeneous output

by hiring high and low-skilled workers. In order to keep the skill hiring decision tractable, we impose some assumptions on the timing of the events. In the beginning of period t, a job separation shock,  $\delta_t$ , is realized. Workers who lose their jobs add to the stock of unemployment from the previous period, forming two different pools of job seekers,  $u_t^h$  and  $u_t^\ell$ , which denote unemployment for high and low-skilled workers respectively.

Firms create new vacancies for high and low skilled workers,  $v_t^h$  and  $v_t^\ell$ , according to a free entry condition. The job seekers match with the vacancies in the labor market, with the number of new matches  $(m_t^h \text{ and } m_t^\ell)$  determined by a matching technology. Production then takes place in two sectors: (i) commodity sector (constrained by SAM frictions), and (ii) consumption good sector (not constrained by any frictions). Total consumption will be a bundle composed by the consumption good and part of the commodity good. The pool of employed workers at the end of the period is carried over to the next period and the same sequence of economic activities takes place.

# 4.1 Labor Market Search and Matching in the commodity sector

In the beginning of period t, there are  $N_{t-1}^h$  and  $N_{t-1}^\ell$  existing job matches, for high and low-skilled workers respectively. A job separation shock displaces a fraction  $\delta_t$  of those matches for every worker type, so that the measure of unemployed job seekers by worker type is given by

$$u_t^{\ell} = \pi x - (1 - \delta_t) N_{t-1}^{\ell},\tag{1}$$

and

$$u_t^h = (1 - \pi)x - (1 - \delta_t)N_{t-1}^h \tag{2}$$

where we have assumed that each worker type in the household has full labor force participation, and the size of the total labor force (high-skilled plus low-skilled workers) is normalized to one.

The job separation rate shock,  $\delta_t$ , is the same for each worker type, and follows the stationary stochastic process

$$\ln(\delta_t) = (1 - \rho_\delta) \ln(\delta) + \rho_\delta \ln(\delta_{t-1}) + \varepsilon_{\delta,t}, \tag{3}$$

where  $\rho_{\delta}$  is the persistence parameter and the term  $\varepsilon_{\delta,t}$  is an i.i.d normal process with zero mean and a standard deviation of  $\sigma_{\delta}$ . The term  $\bar{\delta}$  denotes the steady state rate of job separation.

New job matches are formed between job seekers and open vacancies according to two different sub-markets, one for high-skilled workers and vacancies, and other for low-skilled workers and vacancies. The respective matching functions are

$$m_t^h = \mu_h (u_t^h)^\alpha (v_t^h)^\alpha \tag{4}$$

and

$$m_t^\ell = \mu_\ell (u_t^\ell)^\alpha (v_t^\ell)^\alpha, \tag{5}$$

where  $\mu_h$  and  $\mu_\ell$  are the scale parameters that measures the matching efficiency for high and low-skilled sub-markets, respectively, and  $\alpha \in (0, 1)$  is the elasticity of job matches with respect to the number of job seekers, which we keep the same for both sub-markets, to keep things simple.

The flow of new job matches adds to the employment pool, whereas job separations subtract from it. Aggregate high-skilled employment evolves according to the law of motion

$$N_t^h = (1 - \delta_t) N_{t-1}^h + m_t^h, \tag{6}$$

whereas aggregate low-skilled employment follows the following law of motion

$$N_t^{\ell} = (1 - \delta_t) N_{t-1}^{\ell} + m_t^{\ell}.$$
(7)

At the end of period t, searching workers who failed in finding a job match remain unemployed. Thus, high-skilled unemployment is given by

$$U_t^h = (1 - \pi)x - N_t^h, (8)$$

and low-skilled unemployment is given by

$$U_t^\ell = \pi x - N_t^\ell. \tag{9}$$

Finally, we define the job finding probability for high-skilled workers as

$$p_t^h = m_t^h / u_t^h, (10)$$

and the job finding probability for low-skilled workers as

$$p_t^\ell = m_t^\ell / u_t^\ell. \tag{11}$$

In similar fashion, the job filling probability for high-skilled vacancies is defined as

$$q_t^h = m_t^h / v_t^h, (12)$$

and the job filling probability for low-skilled vacancies is defined by

$$q_t^\ell = m_t^\ell / v_t^\ell,\tag{13}$$

#### 4.2 The Firms in the commodity sector

A continuum of perfectly competitive firms produce a commodity good  $Y_t^{co}$  using high-skilled and low-skilled labor,  $N_t^k$ , as inputs. We assume that all firms behave symmetrically and suppress firm-specific indices. Firms choose their desired number of workers,  $N_t^k$ , and the number of vacancies,  $v_t^k$ , to be posted, by solving the firms's problem, defined by:

$$\mathcal{V}(N_{t}^{h}, N_{t}^{\ell}) = \max_{N_{t}^{h}, N_{t}^{\ell}, v_{t}^{h}, v_{t}^{\ell}} p_{t}^{co} F(N_{t}^{h}, N_{t}^{\ell}) - \sum_{k \in \{h, \ell\}} (w_{t}^{k} N_{t}^{k} + \kappa^{k} v_{t}^{k}) + \mathbb{E}_{t} [\Lambda_{t+1} \mathcal{V}(N_{t+1}^{h}, N_{t+1}^{\ell})]$$
(14)

subject to

$$N_t^k = (1 - \delta)N_{t-1}^k + m_{t-1}^k, \ k \in \{h, \ell\},$$
(15)

where  $\Lambda_{t+1} = \beta \theta_{t+1} (C_{t+1}/C_t)$  is the stochastic discount factor of the households. The real price of the commodity good,  $p_t^{co}$  is taken as given by the firm. Posting vacancies has a unit cost of  $\kappa^k$ .

The production function,  $F(N_t^h, N_t^\ell)$ , is defined by

$$F(N_t^h, N_t^\ell) = Y_t^{co} = Z_t (HN_t^h)^{\alpha_h} (N_t^\ell)^{1-\alpha_h},$$
(16)

where  $Z_t$  denotes a technology shock, and H is an idiosyncratic productivity parameter for high-skilled workers such that H > 1, and  $\alpha_h \in (0, 1)$  is a skillintensity parameter. The technology shock  $Z_t$  follows the stochastic process

$$\ln Z_t = (1 - \rho_z) \ln(\bar{Z}) + \rho_z \ln Z_{t-1} + \varepsilon_{z,t}.$$
(17)

The parameter  $\rho_z \in (-1,1)$  measures the persistence of the technology shock. The term  $\varepsilon_{z,t}$  is an i.i.d normal process with zero mean and finite variance  $\sigma_z^2$ . The term  $\overline{Z}$  is the steady state level of the technology shock.

The first-order condition of the firms' problem with respect to  $v_t^{\ell}$  yields the value function for an open low-skilled vacancy,  $V_t^{\ell}$ , which satisfies the Bellman equation

$$V_t^{\ell} = -\kappa_{\ell} + q_t^{\ell} \mathbb{E}_t [\Lambda_{t+1} (1 - \delta_{t+1}) J_{t+1}^{\ell} + \delta_{t+1}) V_{t+1}^{\ell}].$$
(18)

Analogously, the first-order condition of the firms' problem with respect to  $v_t^h$  yields the value function for an open high-skilled vacancy,  $V_t^h$ , which satisfies the Bellman equation

$$V_t^h = -\kappa_h + q_t^h \mathbb{E}_t [\Lambda_{t+1} (1 - \delta_{t+1}) J_{t+1}^h + \delta_{t+1}) V_{t+1}^h].$$
 (19)

Equations (18) and (19) capture the fact that since hiring is costly, firms spread employment adjustment over time. Firms that hire workers today reap benefits in the future since lower hiring costs can be expended otherwise. In this sense, equations (18) and (19) link the expected benefit of a vacancy in terms of the marginal value of hiring a worker,  $J_t^k$ , to its cost, given by the left-hand side. This is adjusted by the vacancy filling probability,  $q_t^k$ . This is, firms are more willing to post vacancies as the higher the probability is that they can find a worker.

On the other hand, the first-order condition of the firms' problem with respect to  $N_t^{\ell}$  yields the value function for low-skilled employment,  $J_t^{\ell}$ , which satisfies the Bellman equation

$$J_t^{\ell} = p_t^{co} \frac{(1 - \alpha_h) Y_t^{co}}{N_t^{\ell}} - w_t^{\ell} + \mathbb{E}_t \Lambda_{t+1} [\delta_{t+1} V_{t+1}^{\ell} + (1 - \delta_{t+1}) J_{t+1}^{\ell}], \qquad (20)$$

Analogously, the first-order condition of the firms' problem with respect to  $N_t^h$  yields the value function for high-skilled employment,  $J_t^h$ , which satisfies the Bellman equation

$$J_t^h = p_t^{co} \frac{\alpha_h Y_t^{co}}{N_t^h} - w_t^h + \mathbb{E}_t \Lambda_{t+1} [\delta_{t+1} V_{t+1}^h + (1 - \delta_{t+1}) J_{t+1}^h], \qquad (21)$$

Together, equations (18)-(21) and using the standard free-entry condition of search and matching literature,  $V_t^k = 0$ , yield the job creation condition for high and low-skilled workers, respectively, defined by

$$\frac{\kappa_h}{q_t^h} = \mathbb{E}_t \bigg[ \Lambda_{t+1} (1 - \delta_{t+1}) \bigg( p_{t+1}^{co} \frac{\alpha_h Y_{t+1}^{co}}{N_{t+1}^h} - w_{t+1}^h + \frac{\kappa_h}{q_{t+1}^h} \bigg) \bigg],$$
(22)

and

$$\frac{\kappa_{\ell}}{q_{t}^{\ell}} = \mathbb{E}_{t} \bigg[ \Lambda_{t+1} (1 - \delta_{t+1}) \bigg( p_{t+1}^{co} \frac{(1 - \alpha_{h}) Y_{t+1}^{co}}{N_{t+1}^{\ell}} - w_{t+1}^{\ell} + \frac{\kappa_{\ell}}{q_{t+1}^{\ell}} \bigg) \bigg], \qquad (23)$$

The left-hand side captures effective marginal hiring costs, which a firm trades off against the surplus over wage payments it can appropriate and against the benefit of not having to hire someone next period.

#### 4.3 Consumption good sector

The economy has a consumption good sector which produces a good that is consumed by the household domestically. That is, the whole consumption good production is consumed internally. In order to keep things simple, we assume that the consumption good sector labor market is not subject to search frictions, which means that there is full employment in the sector. In other words, as it was stated earlier, if x is the share of household workforce that belong to the commodity sector, then (1-x) is the share of household workforce that belongs to the consumption good sector. As there are no search frictions in this sector, the full workforce (1-x) is employed in production activities for the consumption good. Specifically, consumption goods are produced according to the following production function

$$Y_t^c = Z_t(1-x) \tag{24}$$

#### 4.4 The Representative Household

The representative household has the utility function

$$\mathbb{E}_t \bigg[ \sum_{t=0}^{\infty} \beta^t \Theta_t (ln(C_t) - \chi(N_t^h + N_t^\ell)) \bigg],$$
(25)

where  $\mathbb{E}[\cdot]$  is an expectation operator,  $C_t$  denotes the household consumption, and  $N_t^k$  denotes the fraction of k-skilled household members who are employed, where k = h is to denote high-skilled members, and  $k = \ell$  is to denote low-skilled members. The parameter  $\beta \in (0, 1)$  denotes the subjective discount factor, and the term  $\Theta_t$  denotes an exogenous shifter to the subjective discount factor.

The discount factor shock  $\theta_t = \frac{\Theta_t}{\Theta_{t-1}}$  follows the stationary stochastic process

$$\ln \theta_t = \rho_\theta \ln \theta_{t-1} + \varepsilon_{\theta,t},\tag{26}$$

where  $\rho_{\theta}$  is the persistence parameter and  $\varepsilon_{\theta,t}$  is an i.i.d normal process with zero mean and standard deviation  $\sigma_{\theta}^2$ .

The representative household chooses consumption,  $C_t$ , foreign debt,  $D_t^*$ , and the fraction of high and low-skilled household members that are employed, in order to maximize the utility function (24) subject to the sequence of budget constraints

$$C_t + D_t^* = r_t D_{t-1}^* + w_t^h N_t^h + w_t^\ell N_t^\ell + \phi(x - N_t^h - N_t^\ell), \forall t \ge 0, \qquad (27)$$

where  $r_t$  denotes the interest rate that is carried by the foreign debt, and  $\phi$  measures the unemployment benefits, which we assume are the same for high and low-skilled workers within the household.

The interest rate at which the representative household in the small open economy borrows internationally is given by

$$r_t = a + z_t^r + \psi(e^{D_t^* - D^*} - 1), \tag{28}$$

where a is a constant world interest rate, and  $z_t^r + \psi(e^{\hat{D}_t^* - \bar{D}^*} - 1)$  is a country spread over r. The first term of the spread,  $z_t^r$ , fluctuates exogenously which follows an AR(1) stochastic process, whereas the second term depends on the average household debt,  $\hat{D}_t^*$ , which households take as exogenous. As  $\hat{D}_t^*$  exceeds its steady state level,  $\bar{D}^*$ , the interest rate increases. Finally, the parameter  $\psi > 0$  governs the sensitivity of the interest rate to deviations of debt from the steady state level. The exogenous term of the spread,  $z_t^r$ , follows the following process

$$\ln(z_t^r) = (1 - \rho_{zr}) \ln(\bar{z}^r) + \rho_{zr} \ln(z_{t-1}^r) + \varepsilon_{t,zr}.$$
(29)

Denote by  $B_t(D_t^*, N_t^h, N_t^\ell)$  the value function for the representative household. The household's problem is to maximize the following Bellman equation

$$B_t(D_t^*, N_t^h, N_t^\ell) = \max_{C_t, N_t^h, N_t^\ell, D_t^*} ln C_t - \chi(N_t^h + N_t^\ell) + \beta \mathbb{E}_t \theta_{t+1} B_{t+1}(D_{t+1}^*, N_{t+1}^h, N_{t+1}^\ell)$$
(30)

subject to the budget constraint (27) and the employment laws of motion for high and low skilled workers, (6) and (7).

#### 4.5 Nash bargaining wage

When a job match is formed, regardless if it involves a high or a low-skilled worker, the wage is determined by Nash bargaining. The bargaining wage optimally splits the surplus of a job match between the worker and the firm. Let  $S_t^k$  denote the type-k worker's employment surplus . The firm surplus is given by  $J_t^k - V_t^k$ , and it depends on the employed worker's type,  $k \in \{h, \ell\}$ . The Nash bargaining problem between a firm and a type-k worker is then given

The Nash bargaining problem between a firm and a type-k worker is then given by

$$\max_{w_t^k} (S_t^k)^b (J_t^k - V_t^k)^{1-b},$$
(31)

where  $b \in (0, 1)$  denotes the bargaining power for workers, which is the same within workers' types.

Solving the problem, the Nash bargaining wage for a type-k worker,  $w_t^k$ , satisfies the Bellman equation

$$\frac{b}{1-b}(J_t^k - V_t^k) = w_t^k - \phi - \frac{\chi}{\Lambda_t} + \mathbb{E}_t \Lambda_{t+1} (1 - q_{t+1}^k) (1 - \delta_{t+1}) \frac{b}{1-b} (J_{t+1}^k - V_{t+1}^k)$$
(32)

The closed form solution for wages,  $w_t^h$  and  $w_t^\ell$  is given by

$$w_t^h = b^h \underbrace{(p_t^{co} \frac{\alpha_h Y_t^{co}}{N_t^h} + \kappa_h \theta_h)}_{\text{PMg-h + hiring costs}} + (1 - b^h) \underbrace{(\phi + \chi^h C_t)}_{\text{Outside option}}$$
(33)

and,

$$w_t^{\ell} = b^{\ell} \underbrace{(p_t^{co} \frac{(1 - \alpha_h) Y_t^{co}}{N_t^{\ell}} + \kappa_\ell \theta_\ell)}_{\text{PMg-}\ell + \text{hiring costs}} + (1 - b^{\ell}) \underbrace{(\phi + \chi^\ell C_t)}_{\text{Outside option}}$$
(34)

As is typical in models with surplus sharing, the wage is a weighted average of the payments accruing to workers and firms, with each party appropriating a fraction of the other's surplus, that is determined by workers' Nash bargaining power parameter,  $b^k$ . The bargained wage also includes hiring costs, which are the mutual compensation for costs incurred by the search process, and the utility cost of working,  $\chi^k$ . Besides, the bargaining weight,  $b^k$ , determines how close the wage is to either the marginal product or to the outside option of the worker, the latter of which has to components, unemployment benefits,  $\phi$ , and the consumption utility of leisure,  $\chi^k C_t$ .

#### 4.6 Commodity price and production

The commodity supply is given by the commodity production function defined earlier

$$Y_t^{co} = F(N_t^h, N_t^\ell), \tag{35}$$

which describes the commodity production in each period. We assume that a fraction  $\gamma \in (0, 1)$  of the commodity good is consumed by the households. That is, a fraction  $\gamma$  of the commodity production is consumed by the households, while the remaining fraction,  $(1 - \gamma)$  is exported. Commodity price is denoted by,  $p_t^{co}$ , which is an international price, that is, it is not determined by the commodity producers. This price evolves exogenously by the following AR(1) stochastic process

$$\ln(p_t^{co}) = (1 - \rho_{p^{co}}) \ln(\bar{p}^{co}) + \rho_{p^{co}} \ln(p_{t-1}^{co}) + \varepsilon_{t,p^{co}}, \tag{36}$$

where the parameter  $\rho_{p^{co}} \in (-1, 1)$  measures the persistence of the commodity price shock. The term  $\varepsilon_{t,p^{co}}$  is an i.i.d normal process with zero mean and finite variance  $\sigma_{p^{co}}^2$ . The term  $\bar{p}^{co}$  is the steady state level of the commodity price.

Given the latter, commodity profits are defined by the expression  $\Pi_t^{co} = p_t^{co} Y_t^{co}$ . As it is standard in small open economy models, it is assumed that there is a government which perceives a fraction of the commodity profits. Here we leave that feature aside because we want to analyze a direct channel of commodity shock propagation into the labour market outcomes, and not the effect that goes through an increase of the aggregate demand which arises from the positive impact of the commodity price shock in government consumption.

#### 4.7 Government policy

The government finances unemployment benefit payments,  $\phi$ , for unemployed workers through lump-sum taxes. We assume that the government balances the budget in each period such that

$$T_t = \phi(x - N_t^h - N_t^\ell). \tag{37}$$

#### 4.8 Market clearing and search Equilibrium

We can define the trade balance as

$$TB_t = (1 - \gamma)p_t^{co}Y_t^{co}.$$
 (38)

Consumption spending has to be equal to consumption goods production plus the fraction of the commodity good that is consumed by the households. That is,

$$C_t = Y_t^c + \gamma Y_t^{co}.$$
(39)

Goods market clearing requires that consumption spending, vacancy posting costs, and the trade balance add up to the aggregate production. This requirement yields the aggregate resource constraint

$$Y_t = C_t + \sum_{k \in \{h,\ell\}} \kappa_k v_t^k + TB_t.$$

$$\tag{40}$$

Finally, the net foreign asset position evolves according to

$$D_t^* = r_t D_{t-1}^* + TB_t. (41)$$

# 5 Parametrization Strategy

Our empirical strategy is a mix of both calibrated and estimated parameters. The principal goal when calibrating a subset of parameters is to match steadystate observations and the empirical literature. Afterwards, we estimate the remaining structural parameters and some shock processes in order to fit Chilean time-series data.

#### 5.1 Steady-state and parameter calibration

The model is calibrated using data for Chile at a quarterly frequency. A subset of parameters take values commonly found in the literature for small open economies and DSGE's with SAM frictions, others are calibrated so that the steady state of the model reproduces features for Chile, and the parameters that govern the exogenous processes that drive aggregate fluctuations are estimated using Bayesian techniques, as we will detail in the next section.

The calibrated parameters and targeted steady state values are summarized in Table 1. Going into detail, the unemployment benefit was assumed to be the same between workers' types and equal to 0.25, according to Leduc and Liu (2019)[18]. Regarding fixed worker shares, first the share of commodity workers in the representative household, x, was calibrated to match the statistics of the 2017 wave of CASEN survey for the share of workers who belong to the mining sector in Chile, which is near of a 5% of the total workforce. Second, the share

of low-skilled workers in the economy is, according to the 2017 wave of CASEN survey, approximately 67.6%, which was the value that we used to calibrate the value of  $\pi$ . The elasticity of the matching function,  $\alpha$ , is assumed to be the same for high and low-skilled workers, and we took the value estimated for this parameter in Guerra-Salas et.al (2018), that is,  $\alpha = 0.516$ . Workers, matching efficiency was calibrated in order to capture asymmetric SAM frictions between workers with different skills. They were assumed such that  $\mu_h > \mu_\ell$ , in line with the evidence in Barnichon and Figura (2015)[2], Wolcott (2018), Eeckhout and Kircher (2018)[9] and Dolado et.al., (2021)[7], where the three first aforementioned studies propose a theory of the labor market where firms choose both the size and quality of the workforce, and show that, in a competitive search equilibrium with large firms, high-skilled workers enjoy higher matching probabilities than less-skilled workers. On the other hand, Dolado et.al (2021)[7] calibrates matching efficiencies in order to help the calibration of the remaining parameters; we follow this same approach for these parameters.

Table 1: Calibrated parameters

	Parameter Description	Value	Source		
β	Households subjective discount factor	0.9766	Endogenous		
$\phi$	Unemployment benefit	0.25	Leduc and Liu (2019)		
x	Share of commodity workers in the household	5%	CASEN survey		
α	Elasticity of matching	0.516	Guerra-Salas et.al (2018)		
$\alpha_h$	Skill-intensity parameter for the commodity production	0.43/0.32	Dolado et.al., (2021)/ Benguria, Saffie and Urzua (2018)		
$\mu_h$	h-workers matching efficiency	0.62	Barnichon and Figura (2015); Wolcott (2018)		
$\mu_{\ell}$	ℓ-workers matching efficiency	0.5	Barnichon and Figura (2015); Wolcott (2018)		
$\kappa_h$	h-vacancies posting cost	0.2	Endogenous		
$\kappa_{\ell}$	ℓ-vacancies posting cost	0.1	Endogenous		
$\bar{\delta}^{\kappa_{\ell}}$	Mean value for the separation rate	0.08	Jones and Naudon (2009)		
H	h-workers idiosyncratic productivity	1.7	Endogenous		
π	ℓ-workers proportion within the household	0.676	CASEN survey		
$U^{\ell}/\pi x$	$\ell$ -workers unemployment rate in SS (% of $\ell$ – workforce)	0.08	-		
$U^{h}/(1-\pi)x$	h-workers unemployment rate in SS (% of h-workforce)	0.08	-		
$\chi^h$ $\chi^\ell$ $b^h$	h-workers disutility from working	0.2856	Endogenous		
$\chi^{\ell}$	ℓ-workers disutility from working	0.0998	Endogenous		
$b^h$	h-workers Nash bargaining power	0.65	Cahuc et.al (2006), CASEN survey		
$b^{\ell}$ $\bar{Z}$	ℓ-workers Nash bargaining power	0.58	Cahuc et.al (2006), CASEN survey		
$\overline{Z}$	Mean value for the technology shock	1	Leduc and Liu (2019)		
$\bar{p}^{co}$	Mean value for the copper price shock	1	-		
r	World interest rate (annual)	1%	Guerra-Salas (2017)		
$\bar{z}^r$	Annual steady state EMBI spread 2005-2019	1.4%	BCCh		
$\psi$	Risk premium parameter	0.0007	Guerra-Salas (2017)		
$\overline{TB}/Y$	Trade Balance-to-GDP ratio	0.03	Endogenous		
$\bar{w}_h/\bar{w}_\ell$	Steady State wage premium	1.59	Data		
$\rho_{zr}$	Spread persistence	0.69	Guerra-Salas (2017)		
$\sigma_Z$	std.dev of technology shock	0.035	- ` ´		
$\sigma_{zr}$	std.dev of spread shock	0.17	Guerra-Salas (2017)		

Vacancy posting costs are different between high and low-skilled workers. We did not use any calibration of these parameters in the literature because, to our knowledge, there is little evidence on this, and no direct evidence for Chile. Dolado et.al (2021)[7] presents these parameters, but they assume homogeneity in vacancy posting costs for high and low-skilled workers. Despite of the latter, there is evidence that vacancy posting costs vary by skill. Dube et al. (2010)[8] estimates replacement costs in California are \$2,500 (in 2013 dollars) for blue collar workers and \$8,800 (in 2013 dollars) for professional workers. This includes the cost of recruitment, selection, screening, learning on the job, and separation. Wolcott (2020)[24] takes this evidence and estimates that  $\kappa_h = 0.6$  and  $\kappa_\ell = 0.2$ . Besides, intuitively we may consider that, as there

are less high than low-skilled workers in the economy, the vacancy posting cost of a high-skilled vacancy is higher, because the effort of a firm in finding a highskilled worker qualified to fill the offered vacancy will be higher as there are less unemployed workers of this type in the economy. Also, having an unfilled highskilled vacancy may result in higher losses of productivity in comparison with a low-skilled vacancy, since high-skilled workers are supposed to have higher productivity rates. We used the latter reasoning joint with the calibration of H, which is the parameter that measures h-workers idiosyncratic productivity, to target the steady state value for the wage premium  $(\bar{w}_h/\bar{w}_\ell)$  which, according to the data for 2005-2019 in the UI database, is approximately 1.59. Regarding the mean value for the separation shock,  $\delta$ , we follow Jones and Naudon (2009)[16], who calculate a probability of changing status from employed to unemployed of about 0.04, as well as a probability of changing status from unemployed to employed of about 0.47. These probabilities imply a value for  $\delta$  of about 7.5%, which is at the lower end of the range of quarterly U.S worker separation rates of 8 to 10% reported by Hall (1995) and the values typically used in the literature (Guerra-Salas et.al., (2021)[13]).

We target a steady state unemployment rate for both types of workers. We do this by following the SONAMI (Sociedad Nacional de Minería) report, based on the ENE (Encuesta Nacional de Empleo) survey conducted by the National Statistics Institute (INE) in the 4th quarter of 2019. The report states that mining regions in Chile have approximately 7.8% of unemployment on average, where there is little variation amongst different regions. For example, for Antofagasta, which is the mining capital in Chile, the unemployment rate for the period is 7.5%, Atacama has a 7.7% and Coquimbo registers an 8% of unemployment. Based on this information, we decided to calibrate the steady state unemployment rate for both worker types to 8%, which is a higher bound according to the information of the SONAMI report. As we could not disentangle the unemployment rate for different worker types according to their skill (education) level, we assume that the unemployment rate is the same for high and low-skilled workers. Despite the latter, related literature uses that separation rates should differ between workers of different skill levels, where the parameter for high-skilled workers should be lower than that for low-skilled workers (Dolado et.al., (2021)[7]).

For the Nash bargaining power parameters we used two different -but complementarycriteria in order to do the calibration. First, we look at the related literature (Cahuc et.al., (2006)[5]; Dolado et.al., (2021)[7]) where it is used that the Nash bargaining power parameter for high-skilled workers is higher than that for lowskilled workers. This means that that high-skilled workers perceive a higher share of the surplus that is created by an employment relationship between a firm and a worker, comparing with the share of the surplus that low-skilled workers obtain when bargaining with the firm. While this may be a generalized fact among a wide range of firms and productive sectors, it may not be for a highly unionized economic sector as is mining in Chile. According to the 2017 CASEN survey, 33.54% of mining workers participate in some way in a workers' union, which represents the higher percentage of unionized workers among all economic sectors in Chile. We consider that this fact is important in the wage determination of the mining sector, as bigger workers unions can coordinate pressure activities (as, e.g., strikes) in a better way than smaller ones, which will have an impact in workers' salaries and other working conditions. In addition, we made a descriptive analysis with 2017 wave of CASEN survey and we obtained that 36.8% and 30.65% of high and low-skilled workers<sup>5</sup> belong to a workers union in the mining sector, respectively. These numbers imply that the proportion of high to low skilled workers in a workers' union is close to 48%. This same exercise using the CASEN survey for the year 2015 yields that 34.22%and 32.71% high and low-skilled workers belong to a workers' union, implying that the proportion of high-skilled workers in mining workers' union is a  $40\%^6$ . Summarizing, we calibrate  $b^k$  for  $k \in \{h, \ell\}$ , such that  $b^k > 0.5$ , which is the standard value in search literature, trying to capture the fact of the high share of unionized workers in the mining sector will imply a higher bargaining power for these workers, and that  $b^h > b^\ell$  by a slight margin, trying to capture that union shares between different skilled workers are not so different, and being consistent with the literature mentioned above.

### 6 Estimation

The parameters that govern the exogenous processes that act as driving forces of fluctuations in the model economy are estimated using Bayesian techniques. For this purpose, we use HP filtered series of quarterly data and log demeaned for h and  $\ell$  real wage rates for the mining sector, consumption and real GDP, which are used as observable variables. Wage series were extracted from the unemployment insurance database, whereas consumption and real GDP series were obtained from the Central Bank of Chile Statistics Database. The series time span is from 2005:Q1-2019:Q4. The prior and posterior distributions of the estimated parameters from the model are displayed in Table 2.

The priors are fairly loose, with a Beta distribution with mean 0.7 and standard deviation 0.1 assumed for coefficients  $\rho_{p_{co}}$ ,  $\rho_{\theta}$ ,  $\rho_Z$  and  $\rho_{\delta}$ , and an Inverse Gamma distribution with mean 0.01 and infinite standard deviation for coefficients  $\sigma_{co}$ ,  $\sigma_{\theta}$  and  $\sigma_{\delta}$ . The posterior densities are quite different from the priors, which means that the observed variables are informative about the parameters that drive the exogenous processes. Also, there are three parameters associated to the shock processes that were not estimated, which are the persistence of the spread shock, and the standard deviations for the technology and the spread shocks. The reason that we decided not to estimate these parameters was because of identification issues for them conditional to the observed variables that we use for the estimation. Given the latter, these parameters were calibrated

 $<sup>^5\</sup>mathrm{H}\text{-skilled}$  workers were considered to have some college or superior education, while L-skilled workers were assumed to have non superior education.

 $<sup>^{6}</sup>$ Looking at the proportions of unionized workers outside the Chilean mining sector we have that for 2015 and 2017 those values were equal to 35% and 39%, respectively.

according to the information in Table 1.

		Priors		Posteriors	
	Parameter description	Type	[mean, std]	Mean	90% HPDI
$ ho_{p_{co}}$	Copper price shock persistence	Beta	[0.7, 0.1]	0.5861	[0.4529, 0.7263]
$ ho_{ heta}$	Preference shock persistence	Beta	[0.7, 0.1]	0.8509	[0.7693, 0.9354]
$\rho_Z$	Tech.shock persistence	Beta	[0.7, 0.1]	0.7621	[0.6449, 0.8854]
$\rho_{\delta}$	Job separation shock persistence	Beta	[0.7, 0.1]	0.5306	[0.4117, 0.6438]
$\sigma_{co}$	std of preference shock	Inv.Gamma	[0.01, Inf]	0.5789	[0.4894, 0.6644]
$\sigma_{\theta}$	std of preference shock	Inv.Gamma	[0.01, Inf]	1.5683	[1.2002, 1.9153]
$\sigma_{\delta}$	std of job separation shock	Inv.Gamma	$[0.01,  {\rm Inf}]$	16.983	[14.4133, 19.404]

Table 2: Estimated Parameters

Note: The results are based on 200,000 draws from the posterior distribution using the Metropolis-Hastings (MH) algorithm, dropping the first 100,000 draws in order to achieve convergence. The acceptation rate of the MH algorithm was approximately 25%. HPDI are the highest posterior density intervals. The computations were made using Dynare 4.6.4.

# 7 Analysis of the Model Economy

Based on the calibrated and estimated parameters, we examine the model's transmission mechanism and its quantitative performance in explaining the dynamics of the model, focusing on labor market dynamics. To help understand the contributions of the shocks and the model's mechanism, Section 6.1 examines impulse response functions of non commodity price dynamics, and forecast error variance decomposition, and Section 6.2 examines the dynamics of a commodity price shock individually, and examine how the shock transmission mechanism works in this case, which is our main focus in order to understand how does this kind of impulse affect labor market gaps between high and low-skilled workers.

#### 7.1 Non-Commodity price dynamics

Figure 3 shows the impulse responses of several macro variables to a positive job separation shock. The shock leads to an increase in unemployment for both types of workers, but low-skilled workers are more affected and, therefore, the employment ratio increases. As the overall employment level goes down, there are less inputs to produce commodity, which provokes a fall in aggregate product and in total consumption. Regarding the wage rates, both wages are negatively affected by the job separation shock but, under our parameterization, high-skilled workers are more affected relatively, which yields a decrease in the wage premium as well. Besides, consistently with Shimer (2005)[22], the job separation shock raises both unemployment and vacancies for both types of worker, which mechanically boosts hiring through the matching function<sup>7</sup>.

<sup>&</sup>lt;sup>7</sup>Shimer (2005)[22] argues that the counterfactual implication of the job separation shock for the correlation between unemployment and vacancies renders the shock unimportant for explaining observed labor market dynamics.

Figure 5: IRFs to a shock in  $\varepsilon_{\delta}$ 



Figure 4 shows the impulse responses to a positive technology shock. The shock leads to an increase in both types of employment, but it is low-skilled labor which benefits the most, which results in a decrease in the employment ratio. As employment levels raise, both aggregate production and consumption raise as well. Wages are positively affected, but high-skilled workers see their wage rate increase the most, which leads to an increase in the wage premium.

Figure 6: IRFs to a shock in  $\varepsilon_z$ 



Figure 5 shows the impulse responses to a positive discount factor shock. This shock enters the model through the the job creation condition for both types of workers, leading to a persistent increase on both types of vacancies. As

vacancies go up, both employment levels do as well but, under our parameterization, low-skilled workers benefit more by the shock, leading to a decrease in the employment ratio. Again, wage rates for both worker types increase, but high-skilled workers' wages increase more, which yields a higher wage premium.

Output Consumption Employment ratio 20 20 15 20 Wage premium H-employment leve L-employment level 10 0.0 0.0 0.0 0.02 20 H-wage rate L-wage rate 0.3 0.25 0.2 0.2 0.15 0.1 0.1 0.05 20

Figure 7: IRFs to a shock in  $\varepsilon_{\theta}$ 

#### 7.2 Variance Decomposition

In this section we explore the relative role of the different shocks that we include in the model to explain movements in key variables. We do this by presenting the unconditional forecast error variance decomposition (FEVD) for a selected set of variables.

Table 3 presents the unconditional variance decomposition of a selected set of key variables in the model, using the posterior means for the parameter values and shock innovation sizes presented in Table 2. Aggregate production is mostly explained by the technology shock, followed by the job separation shock, and to a lesser extent by the commodity price shock. The simplistic assumption of fixed labor in the production of the consumption good, and the fact that -in the model- this fixed share of workers represents 95% of total workers makes reasonable that the commodity price shock plays not a great role in aggregate production variation. Despite of the latter, commodity price shocks play a modest role in the literature in explaining the fluctuations of GDP (Guerra-Salas et.al (2021)[13]).

Because of the size of the standard deviation of the job separation shock, it is to be expected that this shock will be considerably important in the fluctuations of many variables of the model. This is specially true for employment levels for both types of workers, where the job separation shock account for more than 93% of the variation of employment for high and low-skilled workers. This contrasts with Shimer (2005)[22], who argues that, in the U.S, job creation is the main cyclical driver of (un)employment. Nevertheless, Elsby, Hobijin and Sahin (2013a) show that in anglo-saxon economies job separation explains near of the 80% of the unemployment variation, whereas in most european countries job separation and job creation fluctuations explain the same share of unemployment variation. Besides, Jakab and Konya (2016)[15] find that separation shocks account for two-thirds of the employment variation in their model. Our result is, therefore, closer to these evidence than to Shimer (2005)[22].

Table 3: Forecast Error Variance Decomposition

Variables	Job separation shock	Technology shock	Discount factor shock	Copper price shock	interest rate shock
Y	21.08	62.46	4.41	12.05	0
$N^h/N^\ell$	92.37	0	7.42	0.21	0
$w^h/w^\ell$	4.88	0.46	25.53	69.13	0
$N_t^h$	93.76	0	6.04	0.2	0
$N_t^\ell$	93.05	0	6.74	0.2	0
$w_t^h$	7.24	0.34	41.06	51.35	0
$w_t^\ell$	8.46	0.28	49.56	41.7	0

Note: The numbers reported are the posterior mean contributions (in percentage terms) of each of the four shocks in the estimation to the forecast error variances of the variables listed in each row.

Despite of the latter, the job separation shock explains a negligible part of the variation of wages, and that of the wage premium, which is consistent with the evidence in Jakab and Konya (2016)[15] and Guerra-Salas et.al (2021)[13]. Discount factor shocks can directly affect the present values of a job match and an open vacancy, and also the employment surplus for a job seeker (Leduc and Liu (2019)[18]). Thus, they are important for explaining the the observed labor market fluctuations (Hall, 2017). Quantitatively, the variance decomposition shows that the discount factor shock contributes to about 45% of the variation of wages, on average, a 25% of the variation in the wage premium, and about a 6% of the variation in employment levels.

The commodity price shock plays, generally, a modest role in the literature. For example, the commodity price shock in Guerra-Salas et.al (2018)[14] explains 6% of GDP variation, 12% of wage variation, and 6% of employment variation. As we endogenized the commodity production, it is natural that the commodity price shock explains a larger fraction of aggregate production and wages in our model, with about a 12% and 45% respectively. Besides, it explains almost a 70% of the wage premium variation in the commodity sector.

Finally, the foreign interest rate shock plays almost no role in explaining the variance of the endogenous variables of our model. This is consistent with the evidence of the role of interest rate spread shocks in Guerra-Salas (2018)[14] and Guerra-Salas et.al (2021)[13].

#### 7.3 Positive shock in the commodity price

Figure 6 shows the dynamic effects of a one-standard-deviation shock to the commodity price. The increase in the commodity price leads to an increase in the aggregate demand, which comes from the increase of commodity production, since the raise in the commodity price has no effect in the dynamics

of the consumption good. As a share of commodity production is consumed by the households, consumption also increases due to the raise in commodity production. Regarding labor market variables, employment for both types of workers increase due to the commodity price shock. This is because job creation conditions for both types of workers increase and, therefore, firms post more vacancies for high and low-skilled workers, which causes that the job creation raises on impact, causing employment to raise as well. Although, the increase in employment is not homogeneous between skill types. We can see from the IRF for the employment rate that the employment for low-skilled workers increases more than the employment for high-skilled workers, which is consistent with our findings in the SVAR exercise in Section 2. Regarding wages, they increase due to the commodity price shock for both types of workers but, this time, those workers who benefit more from the increase of the commodity price are high-skilled workers rather than low-skilled workers. That is, wage rates increase more for high than for low-skilled workers. This can be verified in the IRF for the wage premium, which is positive on impact, and the effect of the commodity price shock vanishes after 10 quarters, approximately.

Figure 8: IRFs to a shock in  $\varepsilon_{p^{co}}$ .



Comparing the result in Figure 2 with the empirical one in Section 2 we have that our model, qualitatively, reproduces well the dynamics found by the SVAR exercise. Despite of this, we are not trying here to match exactly the dynamics showed by the SVAR. This is because we present a rather simple model which has to become more sophisticated in order to match correctly the IRFs in Section 2. Nevertheless, the SVAR results shed light on the intuition that is behind the impact in labor market differences that arise from an exogenous commodity price shock. In this regard, we used the SVAR results to calibrate some structural parameters involving SAM frictions and the skill-intensity in the commodity production, which seem to be appropriate to, at least, replicate qualitatively the empirical evidence.

This result is, somehow, puzzling. Looking into the literature, Guerra-Salas

(2018)[14] shows that a positive impact in commodity prices affects the wage premium and the employment ratio in the same way, specifically, he shows that a positive shock in commodity prices causes the wage premium and the employment ratio to fall, which means that low-skilled workers are more benefited by the price shock regarding wages and employment level. The underlying mechanism of this result is that there is an increase in the relative demand of non-tradable goods with respect to tradable goods. As non-tradable goods are more skill-intensive in low-skilled labor there is a crowding-out effect between both labor types, where workers flow from the tradable to the non-tradable sector which, on aggregate, causes the employment ratio to fall. The latter yields that low-skilled wages go up, and that high-skilled wages go down. In the same fashion but studying a different shock, Dolado et.al., (2021)[7] show that a monetary expansion shock increases the wage premium and the employment ratio, which means that high-skilled workers are the most benefited by the increase in aggregate demand. Considering this evidence, it seems that exogenous shocks that increase aggregate demand (regardless of the source of the shock) causes that the wage premium and the employment ratio move in the same direction, which is not the case here. This is important particularly when comparing with the evidence in Guerra-Salas (2017), where the source of the shock is the same that we emphasize on here and the results, qualitatively speaking, are not the same.

In order to place our results in the literature we have to describe the source of the increase in the wage gap, on the one hand, and the the source of the decrease in employment level gap, which is not clear yet from the analysis we made above. That is, we are not able to state which is the transmission channel of the commodity price shock, this is due to the asymmetric SAM frictions and asymmetric skill-intensity in commodity production that we present in the benchmark version of the model. Therefore, in order to separately identify the effects of asymmetric SAM frictions on the one hand, and skill intensity on the other, we construct next four cases to compare with our benchmark: (i) skill-intensity benchmark and re-calibrating SAM frictions, (ii) SAM frictions benchmark and re-calibrating the skill-intensity parameter, (iii) only asymmetric SAM frictions, and (iv) only skill intensity heterogeneity.

#### 7.3.1 Skill-intensity benchmark

Figure 9 displays the change in the wage premium IRF as H-workers' bargaining power decreases, ceteris paribus. The result is intuitive: the wage premium decreases as H-workers' bargaining power decreases which means, in other words, that as  $\ell$ -workers' relative bargaining power increases, the wage premium will decrease. Also, Figure 9 shows that a 11% decrease in  $b^h$  suffices to have the opposite result regarding the commodity price shock in the wage premium. That is, a 11% decrease in  $b^h$  yields that  $\partial w_t^h / \partial p_t^{co} < \partial w_t^\ell / \partial p_t^{co}$ , thus  $\partial W P_t / \partial p_t^{co} < 0^8$ .

 $<sup>{}^8</sup>WP_t = w_t^h - w_t^\ell$ 

The wage premium decreases monotonically as  $b^h$  decreases.





The other search parameter that is directly related to wages is the vacancy creation cost,  $\kappa_k$ . In order to analyze the wage premium we will consider variations in  $\kappa_\ell$ . The intuition is that as  $\kappa_\ell$  increases, the wage premium is supposed to decrease. Figure 10 shows this exercise and it displays that the latter intuition holds. The wage premium decreases monotonically when  $\kappa_\ell$  increases but at a decreasing rate. The latter implies that even an increase of 400% in  $\kappa_\ell$  can not yield  $\partial W P_t / \partial p_t^{co} < 0$ . This tells us that the wage premium is more sensitive to variations in  $b^h$  than in  $\kappa_\ell$ .

Even though, regarding the calibration section, we stated that the literature stands for  $b^h > b^\ell$  and  $\kappa_h > \kappa_\ell$ , the latter exercise is useful to have some quantitative approach to understand how much must the search parameters increase (or decrease) in order to produce IRF increasing in the opposite direction with respect to the benchmark. In this case, the decrease in  $b^h$  implies a that  $b^h - b^\ell = -0.03$ , which is a feasible difference in bargaining power between high and low-skilled workers since there is no wide consensus in the literature about the magnitude of this difference. The case for  $\kappa_\ell$  is more extreme, because we explored up to a 400% increase in the parameter, which implies that  $\kappa_h/\kappa_\ell = 0.5$ . The latter seems less plausible given what we stated in the calibration section regarding that it should be that  $\kappa_h > \kappa_\ell$ , but it is worth to explore given the quantitative insights that this exercise brings.

Figure 10: Wage premium sensitivity for different  $\kappa_\ell$  and the benchmark skill-intensity,  $\alpha_h$ 



The employment ratio is principally affected by two sub-sets of search parameters:  $\mu_k$  and  $\kappa_k$ , for  $k \in \{h, \ell\}$ . Figures 11 and 12 display the employment ratio comparative statics for  $\mu_h$  and  $\kappa_\ell$ , respectively. Figure 11 shows that the employment ratio increases monotonically when  $\mu_h$  increases, which is consistent with the basic intuition of the matching elasticity parameter; for a given unemployment and vacancy rates, matching efficiency improvements increase the number of matches. Despite of the latter, qualitatively the result stays the same even with a 45% increase of  $\mu_h$  with respect to the benchmark, that is, increasing  $\mu_h = 0.62$  to  $\mu_h = 0.9$ .

Figure 11: Employment ratio sensitivity for different  $\mu_h$  and the benchmark skill-intensity,  $\alpha_h$ 



Finally, Figure 12 shows that increasing  $\kappa_{\ell}$  sufficiently yields that  $\partial W P_t / \partial p_t^{co} > 0$ . The increase must be 4 times the benchmark value of  $\kappa_{\ell}$  for this to happen which, as we stated above, is an unlikely value for this parameter given that it doubles the vacancy posting costs for H-skilled workers. Nevertheless, an increase in  $\kappa_{\ell}$  increases monotonically the employment ratio, since it will become relatively cheaper for firms to create H-vacancies with respect to  $\ell$ -vacancies.

Figure 12: Employment ratio sensitivity for different  $\kappa_{\ell}$  and the benchmark skill-intensity,  $\alpha_h$ 



#### 7.3.2 SAM frictions benchmark

Figures 13 and 14 display the sensitivity of the wage premium and the employment ratio, respectively, with respect to the skill-intensity parameter,  $\alpha_h$ . A 22% decrease in  $\alpha_h$  (w/r to the benchmark) implies that the wage premium IRF decreases about 8 p.p on impact, and it yields that  $\partial W P_t / \partial p_t^{co} < 0$ . The latter implies that the benchmark value of  $\alpha_h = 0.32$  might be a lower bound for the skill-intensity parameter in our framework, in the sense that a slight decrease would yield a wage premium IRF in the opposite direction with respect to our SVAR analysis. Also, increases of  $\alpha_h$  w/r the benchmark value monotonically increases the wage premium, as expected.

Figure 13: Wage premium sensitivity for different  $\alpha_h$  and the benchmark SAM friction parameters



Regarding the employment ratio, it increases monotonically with  $\alpha_h$ , as expected. Making high-skilled workers more important in the production process triggers more hirings for that type of worker, dampening hirings for  $\ell$ -skilled workers.



Figure 14: Employment ratio sensitivity for different  $\alpha_h$  and the benchmark SAM friction parameters

As our model does not include capital it is important to consider in the analysis that, as high-skilled workers should have a higher degree of complementarity with capital than low-skilled workers, making  $\alpha_h$  higher in our framework should be understood as taking account of the capital-skill complementarity that was not modeled here, therefore, it would be likely that  $\alpha_h > 0.32$ , which would imply a higher on-impact value for the wage premium and employment ratio IRFs as displayed in figures 13 and 14. Of course, the right way to assess this is to include capital-skill complementarity to our framework.

#### 7.3.3 Only asymmetric SAM frictions

in this section, in order to understand in a better way the transmission mechanism of our model, we suppress the heterogeneity in skill intensity in the commodity production. Doing so allows us to study what is the effect of changing parameters associated with the SAM frictions in our model and analyze its effects in labor market gaps between high and low-skilled workers. That is, we will assume that  $\alpha_h = 0.5$ , and only focus on variations in the labor market friction parameters of the model, i.e.,  $\mu_k$ ,  $b_k$  and  $\kappa_k$ , with  $k \in \{h, \ell\}$ .

A note here, and which is going to be the case for the rest of the section, is that we will only change one labor market parameter corresponding to one skill type or the other. The reason on doing this exercise is that we want to explore how do labor market gaps change when the baseline conditions in the labor market change as well. That is, we focus on increasing the difference in matching efficiency, bargaining power, and vacancy posting costs, among the different workers' skill types.

Figure 15 shows the IRFs for the employment ratio when the labor market is described by different matching efficiencies. That is, the labor market parameters are the same that are described in Table 1, but we will analyze different IRFs for the employment ratio for the case where  $\mu_{\ell}$  decreases.





From Figure 15, we can observe, first, that the IRF for the employment ratio is still favorable to low-skilled workers when  $\alpha_h = 0.5$ , and the benchmark calibration for the labor market parameters holds. Nevertheless, the situation changes when we increase the difference in matching efficiencies,  $\mu_h - \mu_\ell$ . When  $\mu_\ell$  decreases from the benchmark value, 0.5, to 0.3 it can be observed that the IRF for the employment ratio now increases. The latter implies that a commodity price shock now favors high-skilled workers employment levels. This increasing trend continues when lowering even more the parameter  $\mu_\ell$  to 0.2, where it can be observed that the IRF for the employment ratio increases even more than before because of the commodity price shock. Summarizing, what happens in Figure 7 is consistent with the intuition of standard Search and Matching models that the workers that present less search frictions are those who present higher levels of employment.

Figure 16 shows the IRFs for the wage premium when the labor market is described by different matching efficiencies, as we did above. In this case, with  $\alpha_h = 0.5$ ,  $w_h$  must increase since it is positively related to the skill intensity parameter then, the wage premium for  $\alpha_h = 0.5$  will be higher than the one from the benchmark. Besides, it can be observed that when decreasing  $\mu_{\ell}$  the IRFs for the wage premium decrease as well. The intuition for this is explained by the fact that the wage equations present the marginal productivity of k-labor  $(PMg_k)$ , which is defined by

$$PMg_t^k = \begin{cases} \frac{\alpha_h Y_t^{co}}{N_t^h}, \text{ if } k = h, \\ \\ \frac{(1-\alpha_h)Y_t^{co}}{N_t^\ell}, \text{ if } k = \ell. \end{cases}$$

and when considering  $\alpha_h = 0.5$  this expression becomes
$$PMg_t^k = \begin{cases} \frac{Z_t}{2} \left(\frac{HN_t^\ell}{N_t^h}\right)^{1/2}, & \text{if } k = h, \\ \\ \frac{Z_t}{2} \left(\frac{HN_t^h}{N_t^\ell}\right)^{1/2}, & \text{if } k = \ell. \end{cases}$$

The latter expression shows straightforwardly the result of the wage premium IRF decreasing when the matching efficiency for low-skilled workers decreases as well: with a lower  $\mu_{\ell}$ , low-skilled employment  $(N_t^{\ell})$  increases less than in the benchmark case. This implies that a commodity price shock will have  $PMg_t^h$  increasing less than in the benchmark, and  $PMg_t^{\ell}$  decreasing less than in the benchmark. This yields that when increasing the asymmetries in matching efficiencies, in particular when decreasing  $\mu_{\ell}$  as we do here, the wage premium will decrease by the effect of the Cobb-Douglas production technology, which provokes that high-skilled wage depends positively on low-skilled employment, and that low-skilled wage depends negatively on its self employment level. Despite of the latter, it is worth mentioning that the effect of decreasing  $\mu_{\ell}$  on the wage premium is considerably low, as Figure 8 shows.

Figure 16: IRFs of the wage premium for different matching efficiencies,  $\mu_k$ 



Now turning to study labour market differences when changing the bargaining power differential between workers' types, Figure 17 shows how the wage premium is affected when we increase  $b^h$  above the benchmark value. The blue curve indicates the wage premium dynamics for the benchmark, that is, when  $b^h = 0.65$  and internalizing that  $\alpha_h = 0.5$ . It can be readily seen from Figure 9 that increasing the high-skilled workers bargaining power increases the wage premium as well. The transmission channel that drives this result is that increasing high-skilled workers bargaining power increases their wage rate and,

therefore, a commodity price shock will have a higher impact in  $w_t^h$ , which translates in a higher impact into the wage premium.

Figure 17: IRFs of the wage premium for different H-bargaining power,  $b^h$ 



Figure 18 shows the employment ratio dynamics when having different highskilled vacancy posting costs. In particular, in this exercise we increase  $\kappa_h$  in order to understand how is the employment ratio affected when high-skilled vacancies are more expensive than in the benchmark case. Again, making highskilled vacancies more expensive discourages firms to post this kind of vacancies and, thus, they will crowd-out high-skilled vacancies for low-skilled vacancies. In other words, a higher  $\kappa_h$  provokes that firms post less high-skilled vacancies in benefit of posting more low-skilled vacancies. Since the skill intensity in commodity production is the same for both worker types, firms' only care about the relative cost of posting each type of vacancy. Then, as high-skilled vacancies become expensive, firms will be less willing to post that kind of vacancies, which favors low-skilled employment, pushing the employment ratio to go down, as Figure 18 shows for an increasing  $\kappa_h$ .



15 Quarters

Figure 18: IRFs of the employment ratio for different H-vacancy creation cost,  $\kappa_h$ 

7.3.4 Only skill-intensity heterogeneity in commodity production

Now we turn to the case in which there are not SAM asymmetries, so we can focus in how are labor market outcome gaps affected by a commodity price shock when the skill-intensity in commodity production changes. Specifically, we will revise the case in which the skill-intensity for high-skilled workers increases. With high-skill intensity in commodity production increasing, basically we are saying that the elasticity of high-skilled labor in commodity production is higher and then this kind of workers yields more commodity production by unit hired, compared to low-skilled labor. This case can be compared with the skill-intensity for tradable goods mentioned in Guerra-Salas (2018)[14]. The assumption is basically that, in our framework,  $\alpha_h > 0.32$ , which is the benchmark value. This statement is somewhat related to the Dutch Disease literature, which often assumes the manufacturing tradable sector concentrates learningby-doing, increasing returns to scale, spillover effects, or other positive externalities (van Wijnbergen (1984)[23]; Lama and Medina (2018)[17], García-Cicco and Kawamura (2015)[12]). Though not exactly the same case for the commodity sector, we can relate a high skill-intensity in commodity production to the case where there are capital-skill complementarities in production.



Figure 19: IRFs of the employment ratio for different H-skill intensity in commodity production,  $\alpha_h$ 

Figure 19 shows the dynamics for the employment ratio when increasing the skill-intensity in commodity production. As the high-skilled elasticity in commodity production increases, firms are more willing to hire high-skilled worker. In other words, the value of high-skilled employment increases as  $\alpha_h$  is higher which, at the same time, increases the value of creating a high-skilled vacancy. The latter pushes firms to create high-skilled vacancies and, therefore, high-skilled employment goes up. This result implies that as high-skilled workers become more important in commodity production, they will be more benefited by commodity price shocks than low-skilled workers, which yields a lower employment ratio between workers of different skills.

Finally, Figure 20 shows the dynamics for the wage premium when increasing the skill-intensity in commodity production and shutting down the SAM frictions heterogeneity. First, it is worth noting that when  $\alpha_h = 0.32$  we go back to the neoclassical result where the employment ratio and the wage premium respond in the same direction to a commodity price shock. This is due the fact that workers are homogeneous in their SAM frictions, but the skill-intensity parameter favors  $\ell$ -workers' relative employment and, therefore, their wages. In other words, if different workers face the same labor market institutions, the only important feature driving labor market outcome gaps is the demand channel, which is driven by the skill-intensity in production in our case. Also, it can be readily seen that increasing  $\alpha_h$  favors high-skilled workers wages, where the higher  $\alpha_h$  is, the higher is the effect of a commodity price shock on impact. The effect is not negligible, since increasing  $\alpha_h$  from 0.5 to 0.7 implies an increase of the wage premium IRF on impact of almost twice as much, going from a bit higher than 0.15 to approximately 0.35.



Figure 20: IRFs of the wage premium for different H-skill intensity in commodity production,  $\alpha_h$ 

Summarizing, the results of this section helped us to understand better the shock transmission mechanism that underlies in our model. First, analyzing the case that implies only SAM asymmetries we learned that increasing the gaps regarding labor market conditions that workers' face by changing the labor market parameters calibration favors the type of worker that faces less frictions, which is consistent with the search and matching literature. In this regard, the only result that is, somewhat, counterintuitive is the one that does the sensitivity analysis of the wage premium when increasing the matching efficiency gap, that is, lowering low-skilled workers matching efficiency. Despite the latter, we have that the wage premium decreases because the particular production technology that we use in the model (Cobb-Douglas), which implies that the marginal productivity for high-skilled workers depends positively in low-skilled labor, and the opposite happens for the marginal productivity for low-skilled workers. It would be interesting to analyze if this result holds or not using another production technology, such as one that presents capital-skill complementarities, for example, but this is out of the scope of this paper.

Regarding the skill-intensity channel in the transmission of the commodity price shock, in Section 6.1.2 we showed that increasing the skill-intensity in commodity production favors high-skilled workers instead of low-skilled workers, that is, the commodity price shock increases labor market differences in terms of employment and wages between different types of workers as commodity production becomes more intensive in high-skilled labor.

#### 7.4 Wage Decomposition

In this section we perform a wage decomposition exercise in order to understand which elements of the workers' wages contribute the most to the wage dynamics when there is a commodity price shock. Let us recall that the wage equation for a k-skilled worker is defined by

$$w_t^k = b^k (p_t^{co} P M g_t^k + \kappa_k \theta_k) + (1 - b^k) (\phi + \chi^k C_t), \text{ for } k \in \{h, \ell\}.$$

Here, we can find three endogenous sources of wage variation that arise from a commodity price shock: (i) Marginal productivity of k-skilled labor,  $PMg_t^k$ , (ii) k-skilled labor market tightness,  $\theta_k$ , and (iii) the household utility of leisure in terms of consumption,  $\chi^k C_t$ . The commodity price forms part of the wage dynamics as well, but is an exogenous source of variation. Despite of this, we will consider in the analysis the joint effect of  $p_t^{co}PMg_t^k$  on wage dynamics.

Figures 21 and 22 show the wage decomposition by worker skill type. Starting with Figure 21, it shows the high-skilled workers wage decomposition. It can be seen that the dynamics for  $w_t^h$  are mainly decomposed into two components,  $p_t^{co}PMg_t^h$  and  $\theta_h$ . Here, the most important part for the wage variation is attributed to the increase in the marginal productivity of high-skilled labor times the commodity price shock, which accounts for more than the 80% of the variation on impact. The rest of the wage variation is attributed to the increase in the market tightness. The share of variation that comes from the variation in household leisure utility is negligible. These findings are consistent with the evidence showed in Dolado et.al (2021), where it is documented that the wage decomposition dynamics that arise from a monetary shock come from changes in the firm's surplus.

Figure 21: IRF decomposition for  $w_t^h$ 



Regarding Figure 22, it shows the IRF decomposition for low-skilled workers wage rate,  $w_t^{\ell}$ . The decomposition is quite similar to the one for high-skilled workers, that is, the effect of a commodity price shock in wages is decomposed in, basically, the same two components that explain the variation in wages for high-skilled workers. The difference relies mainly in that, on impact, the share of the variation explained by  $p_t^{co}PMg_t^{\ell}$  is approximately 85%, but the essence of the decomposition is almost the same.

Figure 22: IRF decomposition for  $w_t^{\ell}$ 



Finally, Figure 23 shows the decomposition for the wage premium dynamics.

Again, as in Figures 21 and 22, we have that most of the variation in the wage premium comes from the commodity price impact on aggregate demand pressures. As in Dolado et. al (2021)[7], this suggests that the increase in the wage gap is achieved mostly through changes in the firm's surplus, accounted by  $p_t^{co}(PMg_t^h - PMg_t^\ell)$ , which lead to adjustments in labor demand. The second factor that contributes noticeably is the difference in labor market tightness,  $\theta_h - \theta_\ell$ , but by a much lower extent than aggregate demand pressures. In this regard, contrasting with Dolado et.al (2021)[7] we have here that the impulse in labor market tightness is higher for high-skilled workers than for low-skilled workers. This means that it seems that, for our case, tighter labor markets contribute to increase the wage premium rather to mitigate it, as in Dolado et.al (2021)[7].





### 8 Conclusion

In order to improve our knowledge of the effects that commodity price shocks affect the labor market outcomes of different types of workers and the channels through which these kind of shocks act within the domestic economy, we have built a SOE-DSGE model with skill-intensity in commodity production and asymmetric search-and-matching (SAM) frictions in the labor market between high-skilled and low-skilled workers. The model was calibrated and estimated in order to fit Chilean time series for the period 2005-2019. Our contribution to the literature is to propose a mechanism that takes into account that workers face SAM frictions and how this interacts with external shocks in a SOE environment, where the commodity production is subject to skill-intensity. Our findings show that as skill-intensity in the commodity production falls which, in our environment, means that high-skilled workers become less important in commodity production, labor market gaps decrease as well, but the interaction with SAM frictions, which translates into higher labor market outcomes for the workers face less frictions (high-skilled workers), inhibits the power of the skill intensity to mitigate the wage gap, while it succeeds in decreasing the employment level differences. We have to highlight here that we calibrated the model to fit the data for Chile and in this setup happens that, as commodity production is more skill-intensive in low-skilled labor, SAM frictions in favor of high-skilled workers counteract the effect of our calibrated skill-intensity in commodity production. As Dolado et.al (2021)[7] point out, these findings are not qualitatively specific to commodity price shocks but turn out to be similar for any other type of shocks that increase aggregate demand.

The theoretical model is motivated by a SVAR empirical analysis, in which we have shown that a commodity price shock induces a significant rise in the wage premium, and reduces the employment ratio in the Chilean mining sector. The SVAR analysis shows that employment level differences (measured by the employment ratio between high and low-skilled workers) decreases on impact and this effect is persistent, lasting more than 10 quarters and, regarding the wage gap, it increases on impact and afterwards it tends to decrease, but the positive effect is relatively persistent. This is novel evidence in labor market outcome differences between high and low-skilled workers, using administrative data available in the UI system, which allowed us to handle a considerable amount of worker observations for a relatively long time span, which encompasses the commodity boom period which started in 2002 and lasted to -approximately-2012, and further. In this regard, extant literature only uses data for the commodity boom period, therefore, we add to these evidence with recent data and that covers a longer time span.

Overall, the model reproduces well the findings in the SVAR analysis. Nevertheless, the theoretical model that we proposed is simple, and it can be easily extended in a richer Neo-Keynesian framework, which would allow other channels to act, as the exchange rate channel would do. Also, as in Dolado et. al (2021)[7], our model could be extended allowing that the commodity production to present capital-skill complementarity, which is important in a highly capital-intensive sector as the mining one is. We let these features to further research.

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# 9 Appendix

### 9.1 Tables and plots

Figure 24: IRFs to an unexpected increase in the international copper price.



Note: Calculated using the UI database for the 20% of the whole pool of Chilean mining sector formal workers.

Figure 25: Representative household allocation of labor between productive sectors.



Figure 26: Share of Copper Workers en Chile, 2014-2020



Figure 27: Source: Encuesta Nacional de Empleo (ENE). Instituto Nacional de Estadísticas

## 9.2 Equilibrium conditions (non-linear)

$$1 = \beta \mathbb{E}_t \left[ \theta_{t+1} \, \frac{c_t}{c_{t+1}} \, r_t \right] \tag{42}$$

$$r_t = a + zr_t + \psi \, (\exp \left(D_t - D_{-}ss\right) - 1) \tag{43}$$

$$m_t^\ell = \left(u_t^\ell\right)^\alpha \left(v_t^\ell\right)^{(1-\alpha)} \tag{44}$$

$$q_t^\ell = \frac{m_t^\ell}{v_t^\ell} \tag{45}$$

$$N_t^{\ell} = m_{t-1}^{\ell} + (1 - \delta_t) \ N_{t-1}^{\ell} \tag{46}$$

$$u_t^{\ell} = \pi \, x - (1 - \delta_t) \, N_{t-1}^{\ell} \tag{47}$$

$$U_t^\ell = \pi \, x - N_t^\ell \tag{48}$$

$$m_t^h = \mu^h \left( u_t^h \right)^\alpha \left( v_t^h \right)^{(1-\alpha)} \tag{49}$$

$$q_t^h = \frac{m_t^h}{v_t^h} \tag{50}$$

$$N_t^h = m_{t-1}^h + (1 - \delta_t) \ N_{t-1}^h \tag{51}$$

$$u_t^h = x \ (1 - \pi) - (1 - \delta_t) \ N_{t-1}^h \tag{52}$$

$$U_t^h = x \ (1 - \pi) - N_t^h \tag{53}$$

$$\eta_t^h = \frac{v_t^h}{u_t^h} \tag{54}$$

$$\eta_t^\ell = \frac{v_t^\ell}{u_t^\ell} \tag{55}$$

$$\frac{\kappa_h}{q_t^h} = \beta \mathbb{E}_t \left[ \frac{\theta_{t+1} c_t}{c_{t+1}} \left( 1 - \delta_{t+1} \right) \left( \frac{\alpha_h \, p_{t+1}^{co} \, Y_{t+1}^{co}}{N_{t+1}^h} - w_{t+1}^h + \frac{\kappa_h}{q_{t+1}^h} \right) \right] \tag{56}$$

$$\frac{\kappa_{\ell}}{q_{t}^{\ell}} = \beta \mathbb{E}_{t} \left[ \frac{\theta_{t+1} c_{t}}{c_{t+1}} \left( 1 - \delta_{t+1} \right) \left( \frac{(1 - \alpha_{h}) p_{t+1}^{co} Y_{t+1}^{co}}{N^{\ell}_{t+1}} - w_{t+1}^{\ell} + \frac{\kappa_{\ell}}{q_{t+1}^{\ell}} \right) \right]$$
(57)

$$Y_t^c = Z_t \ (1-x) \tag{58}$$

$$Y_t^{co} = Z_t \left( H N_t^h \right)^{\alpha_h} \left( N_t^\ell \right)^{1 - \alpha_h} \tag{59}$$

$$C_t = Y_t^c + \gamma Y_t^{co} \tag{60}$$

$$Y_t = C_t + v_t^h \kappa_h + v_t^\ell \kappa_\ell + (1 - \gamma) p_t^{co} Y_t^{co}$$

$$\tag{61}$$

$$w_t^h = b_h \left( \frac{\alpha_h \, p_{t+1}^{co} \, Y_{t+1}^{co}}{N_{t+1}^h} + \theta_t^h \, \kappa_h \right) + (1 - b_h) \, (\phi + \chi_h C_t) \tag{62}$$

$$w_t^{\ell} = b_{\ell} \left( \frac{(1 - \alpha_{\ell}) \, p_{t+1}^{co} \, Y_{t+1}^{co}}{N_{t+1}^{\ell}} + \theta_t^{\ell} \, \kappa_{\ell} \right) + (1 - b_{\ell}) \, \left(\phi + \chi_{\ell} C_t\right) \tag{63}$$

$$\log\left(\delta_{t}\right) = (1 - \rho_{\delta})\,\log\left(\bar{\delta}\right) + \rho_{\delta}\,\log\left(\delta_{t-1}\right) + \varepsilon_{\delta t} \tag{64}$$

$$\log\left(Z_t\right) = (1 - \rho_Z)\,\log\left(\bar{Z}\right) + \rho_Z\,\log\left(Z_{t-1}\right) + \varepsilon_{t,Z} \tag{65}$$

$$\log\left(\theta_{t}\right) = \rho_{\theta} \,\log\left(\theta_{t-1}\right) + \varepsilon_{\theta,t} \tag{66}$$

$$\log(p_t^{co}) = (1 - \rho_{p^{co}}) \log(\bar{p}^{co}) + \rho_{p^{co}} \log(p_{t-1}^{co}) + \varepsilon_{t,p^{co}}, \tag{67}$$

$$\log(z_t^r) = (1 - \rho_{zr})\log(\overline{z}^r) + \rho_{zr}\log(z_{t-1}^r) + \varepsilon_{t,zr}.$$
(68)

$$emp\_rate_t = N_t^h - N_t^\ell \tag{69}$$

$$wage\_prem_t = w_t^h - w_t^\ell \tag{70}$$

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